## GCE Examinations

## Advanced Subsidiary

## Core Mathematics C2

## Paper E

## MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks could be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.
Accuracy marks (A) can only be awarded when a correct method has been used.
(B) marks are independent of method marks.


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## C2 Paper E - Marking Guide

1. $=\left[2 x+x^{-1}\right]_{2}^{4}$

M1 A1
$=\left(8+\frac{1}{4}\right)-\left(4+\frac{1}{2}\right)=3 \frac{3}{4}$
M1 A1
(4)
2. $\mathrm{f}^{\prime}(x)=3 x^{2}+8 x-3$
increasing when $\quad 3 x^{2}+8 x-3 \geq 0$
M1 A1
$3 x^{2}+8 x-3 \geq 0$
$(3 x-1)(x+3) \geq 0$
$x \leq-3$ or $x \geq \frac{1}{3}$


M1
M1
A1 (5)
3. (a) $=\log _{2}\left(3^{2} \times 5\right)$

$$
=2 \log _{2} 3+\log _{2} 5=2 p+q
$$

B1
(b) $=\log _{2} \frac{3}{5 \times 2}=\log _{2} 3-\log _{2} 5-\log _{2} 2$

M1 A1

$$
\begin{equation*}
=p-q-1 \tag{6}
\end{equation*}
$$

B1 A1
4. (a) $(1+k x)^{7}=\ldots+\binom{7}{2}(k x)^{2}+\ldots$
$\therefore \frac{7 \times 6}{2} \times k^{2}=525$
$k^{2}=\frac{525}{21}=25$
M1
$k>0 \therefore k=5$
A1
(b) $(1+5 x)^{7}=\ldots+\binom{7}{3}(5 x)^{3}+\ldots$
$\therefore$ coeff. of $x^{3}=\frac{7 \times 6 \times 5}{3 \times 2} \times 125=4375 \quad$ M1 A1
(c) $\begin{array}{ll}(1+5 x)^{7}=1+35 x+525 x^{2}+\ldots & \text { B1 }\end{array}$
$\begin{aligned}(2-x)(1+5 x)^{7} & =(2-x)\left(1+35 x+525 x^{2}+\ldots\right) \\ & =2+70 x+1050 x^{2}-x-35 x^{2}+\ldots \\ & =2+69 x+1015 x^{2}+\ldots\end{aligned}$ A1 (8)
5. (a) $\frac{1}{2} \sqrt{3}$

B1
(b) $\begin{array}{lllll}x & 0 & \frac{\pi}{6} & \frac{\pi}{3}\end{array}$

M1
$\begin{array}{llll}\cos ^{2} x & 1 & \frac{3}{4} & \frac{1}{4}\end{array}$
A1
area $\approx \frac{1}{2} \times \frac{\pi}{6} \times\left[1+\frac{1}{4}+2\left(\frac{3}{4}\right)\right]$
B1 M1

$$
=0.720(3 \mathrm{sf})
$$

A1
(c) area of $S=\int_{0}^{\frac{\pi}{3}} \sin ^{2} x \mathrm{~d} x=\int_{0}^{\frac{\pi}{3}}\left(1-\cos ^{2} x\right) \mathrm{d} x$ M1

$$
=\frac{\pi}{3}-0.71995=0.327(3 \mathrm{sf})
$$

M1 A1 (9)
6. (a) isosceles $\therefore \angle A M B=90^{\circ}$

## B1

$B M=4 \tan 30^{\circ}=\frac{4}{\sqrt{3}}$
M1 A1
area $=\frac{1}{2} \times 8 \times \frac{4}{\sqrt{3}}=\frac{16}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}=\frac{16}{3} \sqrt{3} \mathrm{~cm}^{2}$
M1 A1
(b) area of sector $=\frac{1}{2} \times 4^{2} \times \frac{\pi}{6}=\frac{4}{3} \pi$

B1 M1
shaded area $=\frac{16}{3} \sqrt{3}-\left(2 \times \frac{4}{3} \pi\right)$
M1

$$
=\frac{16}{3} \sqrt{3}-\frac{8}{3} \pi=\frac{8}{3}(2 \sqrt{3}-\pi) \mathrm{cm}^{2}
$$

A1
(9)
7. (a) $(-6,5) \therefore \begin{aligned} & 36+25-60-40+k=0 \\ & k=39\end{aligned}$

M1
A1
(b) $(x+5)^{2}-25+(y-4)^{2}-16+39=0$

M1
$(x+5)^{2}+(y-4)^{2}=2$
$\therefore$ centre $(-5,4)$, radius $=\sqrt{2}$
A2
(c)


$$
\text { dist. }(2,3) \text { to centre }=\sqrt{49+1}=\sqrt{50}
$$

B1
$\begin{array}{rlr}\therefore & A B^{2}=(\sqrt{50})^{2}-(\sqrt{2})^{2}=48 & \text { M1 A1 } \\ & A B=\sqrt{48}=\sqrt{16 \times 3}=4 \sqrt{3} & \text { M1 A1 }\end{array}$
8. (a) end of $1^{\text {st }}$ year: $500 \times 1.06=530$
start of $2^{\text {nd }}$ year: $530+500=1030$
interest at end of $2^{\text {nd }}$ year $=0.06 \times 1030=£ 61.80$
M1 A1
(b) end of $8^{\text {th }}$ year: $500 \times\left(1.06+1.06^{2}+1.06^{3}+\ldots+1.06^{8}\right)$

$$
\begin{aligned}
& =500 \times S_{8} ; \text { GP, } a=1.06, r=1.06 \\
& =500 \times \frac{\left.1.06[1.06)^{8}-1\right]}{1.06-1} \\
& =5245.66 \therefore £ 5246 \text { (nearest pound) }
\end{aligned}
$$

(c) $(1.005)^{12}=1.0617 \ldots$
end of $8^{\text {th }}$ year: $\quad 500 \times \frac{1.0617\left[(1.0617)^{8}-1\right]}{1.0617-1}=5285.71$
$\therefore £ 40$ more in account (nearest pound)
B1
M1 A1
A1
M1 A1
M1 A1
A1
(12)
9. (a)
$\begin{array}{lll}\mathrm{f}(-1)=r & \therefore-1+k+7-15=r \\ & k=r+9 \\ \mathrm{f}(3)=3 r \quad \therefore & 27+9 k-21-15=3 r \\ & 3 k=r+3\end{array}$
M1
A1
M1
subtracting, $\quad 2 k=-6$
M1
$k=-3$
A1
(b) $r=-3-9=-12$ B1
(c) $\mathrm{f}(x)=x^{3}-3 x^{2}-7 x-15$
$\mathrm{f}(5)=125-75-35-15=0 \quad \therefore(x-5)$ is a factor
(d)

$$
\begin{aligned}
& \begin{aligned}
& x^{2}+2 x+3 \\
& \begin{array}{l}
x^{3}-3 x^{2}-7 x-15 \\
x^{3}-5 x^{2} \\
2 x^{2}
\end{array}-7 x
\end{aligned} \\
& \frac{2 x^{2}-10 x}{3 x}-15 \\
& 3 x-15 \\
& \therefore(x-5)\left(x^{2}+2 x+3\right)=0 \\
& x=5 \text { or } x^{2}+2 x+3=0 \\
& b^{2}-4 a c=2^{2}-(4 \times 1 \times 3)=-8 \\
& \text { M1 } \\
& b^{2}-4 a c<0 \quad \therefore \text { no real solutions to quadratic } \\
& \therefore \text { only one real solution }
\end{aligned}
$$

## Performance Record - C2 Paper E

| Question no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic(s) | integr. | $\left.\begin{array}{\|c\|} \hline \text { increasing } \\ \text { function } \end{array} \right\rvert\,$ | logs | binomial | $\begin{array}{\|c} \text { trapezium } \\ \text { rule } \end{array}$ | $\begin{array}{\|c} \text { Sector } \\ \text { Sof a } \\ \text { circle } \end{array}$ | circle | GP | remain. theorem alg. div. aneore, and |  |
| Marks | 4 | 5 | 6 | 8 | 9 | 9 | 10 | 12 | 12 | 75 |
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